9. [6 points]

The implicit curve $\mathcal{C}$ is given by the equation

$$
y^{2}-1=r^{2}+x^{2}(y-r)
$$

for some constant $r$. A graph of the curve with $r=1$ is shown to the right. Note that

$$
\frac{d y}{d x}=\frac{2 x(y-r)}{2 y-x^{2}} .
$$

Answer each of the following questions about the implicit curve $\mathcal{C}$. Your answers must be in exact form.

a. [2 points] When $r=1$, the curve $\mathcal{C}$ passes through the point $(\sqrt{2}, 0)$. Write a formula for the tangent line to the curve $\mathcal{C}$ at this point.

## Answer:

b. [4 points] In this part, we do not assume anything about $r$. In particular, do not assume $r=1$. Find the $(x, y)$ coordinates of all points at which the tangent line to the curve $\mathcal{C}$ is horizontal. If there are no such points, write none. Your answer may be in terms of the constant $r$. You must show every step of your work.

Answer:

