

10. [4 points] An implicit curve is described by the equation

$$xy^n = \cos(ax)$$

where  $a$  and  $n$  are positive constants. Compute  $\frac{dy}{dx}$ . Your answer may include  $a$  and  $n$ . You must show every step of your work.

*Solution:*

$$\begin{aligned} \frac{d}{dx}(xy^n) &= \frac{d}{dx}(\cos(ax)) \\ x \cdot \left( ny^{n-1} \frac{dy}{dx} \right) + 1 \cdot y^n &= -a \sin(ax) \\ (nxy^{n-1}) \frac{dy}{dx} &= -a \sin(ax) - y^n \\ \frac{dy}{dx} &= \frac{-a \sin(ax) - y^n}{nxy^{n-1}} \end{aligned}$$

**Answer:**  $\frac{dy}{dx} = \frac{-a \sin(ax) - y^n}{nxy^{n-1}}$

11. [8 points] The differentiable function  $f(x)$  is defined for all real numbers. Additionally,  $f(x)$  has **exactly two** critical points, at  $x = 0$  and  $x = 5$ . A table of values of  $f(x)$  is given below.

$x$	-2	1	3	7
$f(x)$	2	4	9	5

For parts **a.–d.**, circle **all** correct choices.

- a. [2 points] On which of the following interval(s) must  $f'(x)$  always be negative?

(-2, 0)      (0, 1)      (1, 5)       (5, 7)      NONE OF THESE

- b. [2 points] On which of the following interval(s) must there be a point  $c$  for which  $f'(c) = -1$ ?

$(-\infty, -2)$        $(-2, 1)$        $(1, 3)$         $(3, 7)$       NONE OF THESE

- c. [2 points] On the interval  $[0, 6]$ , at which of the following point(s) does  $f(x)$  attain its global maximum? If there is not enough information to determine this, circle NOT ENOUGH INFO.

$x = 0$        $x = 1$         $x = 5$        $x = 6$       NOT ENOUGH INFO

- d. [2 points] On the interval  $[-2, 5]$ , at which of the following point(s) does  $f(x)$  attain its global minimum? If there is not enough information to determine this, circle NOT ENOUGH INFO.

$x = -2$        $x = 0$        $x = 2$        $x = 5$        NOT ENOUGH INFO