

3. [15 points] Let the differentiable function  $h(t)$  represent the height in inches (in) of a toy airplane above the ground at time  $t$  seconds (sec). Below is a table of some values for  $h(t)$  and  $h'(t)$ . Assume that  $h(t)$  is invertible, and that  $h'(t)$  is differentiable for  $t > 0$ .

$t$	0	2	4	6	8
$h(t)$	28	19	11	8	4
$h'(t)$	-5	-4	-2	-1.5	-0.5

For parts **a.**–**d.**, you do not need to show work, but partial credit can be earned from work shown. You do not need to simplify numerical answers.

- a.** [3 points] Approximate  $h''(8)$ . Include units.

**Answer:** \_\_\_\_\_

- b.** [3 points] Find a formula for the linear approximation  $L(t)$  to the function  $h(t)$  at  $t = 2$ .

**Answer:**  $L(t) =$  \_\_\_\_\_

- c.** [2 points] Use your answer from the previous part to approximate  $h(1.9)$ . Include units.

**Answer:** \_\_\_\_\_

- d.** [2 points] Compute the **exact** value of  $(h^{-1})'(8)$ . (You do not need to include units.)

**Answer:** \_\_\_\_\_

- e.** [3 points] Suppose that  $(h^{-1})'(3) = -9$ . Complete the following sentence to give a practical interpretation of this equation.

*When the toy airplane is at a height of 3 inches, to descend an additional 0.1 inches ...*

- f.** [2 points] Note that  $h(t)$  satisfies the hypotheses of the Mean Value Theorem on  $[0, 8]$ . Complete the following sentence about what the conclusion of this theorem implies is true.

*At some time between  $t = 0$  and  $t = 8$ , the height of the toy airplane is ...*

(circle one)      INCREASING      DECREASING      at a rate of \_\_\_\_\_ in/sec.