

10. [7 points] The curve  $\mathcal{C}$  is given by the equation  $e^{\cos(x^2-y^2)} = ex$ .

a. [2 points] Which of the following points  $(x, y)$  lie on the curve  $\mathcal{C}$ ? Circle all correct answers.

(1, 1)            (-1, 1)            (1, -1)             $(0, \sqrt{2})$             NONE OF THESE

b. [5 points] Compute  $\frac{dy}{dx}$ . Show every step of your work and circle your final answer.

11. [8 points]

Suppose  $h(x)$  is a function such that  $h(x)$  has exactly three critical points. Assume that both  $h(x)$  and  $h'(x)$  are differentiable on  $(-\infty, \infty)$ . A table of values is given to the right.

$x$	0	3	5	7
$h(x)$	2	?	4	4
$h'(x)$	-1	0	0	?

a. [2 points] Note that  $h(x)$  satisfies the hypotheses of the Mean Value Theorem on  $[5, 7]$ . Briefly explain why the conclusion of this theorem implies that one of the three critical points of  $h(x)$  must be in the interval  $5 < x < 7$ .

In the parts below, circle all correct answers. No justification is needed.

b. [2 points] On which of the following intervals *must*  $h(x)$  be increasing on the entire interval?

(0, 3)            (3, 5)            (5, 6)            (6, 7)            NONE OF THESE

c. [2 points] Which of the following *could* be the  $x$ -coordinate of a global minimum of  $h(x)$  on  $(-\infty, \infty)$ ?

$x = 0$              $x = 3$              $x = 5$              $x = 6$             NONE OF THESE

d. [2 points] Also suppose that  $h(x)$  is concave down on  $(-\infty, 0)$ . Which of the following *could* be the value of  $h(-2)$ ?

1            2            3            4            5            NONE OF THESE