

8. [7 points] The function  $f(x)$  is defined as follows:

$$f(x) = \begin{cases} \frac{x}{x^2 + 1} & x \leq 0 \\ ? & x > 0. \end{cases}$$

Note that the formula for  $f(x)$  for  $x > 0$  is unknown. However, it is known that  $f(x)$  is differentiable at each point in its domain  $(-\infty, \infty)$ , and that  $f'(x) > 0$  for all  $x \geq 0$ .

- a. [4 points] Find the  $x$ -coordinates of all global minimum(s) and global maximum(s) of  $f(x)$  **on the interval**  $(-\infty, 0]$ . If there are none of a particular type, write NONE. Use calculus to find your answers, and make sure that you show enough evidence to justify your conclusions.

**Answer:** Global min(s) at  $x =$  \_\_\_\_\_

**Answer:** Global max(es) at  $x =$  \_\_\_\_\_

- b. [3 points] For each question below, circle all correct answers. No justification is needed.

At which of the following value(s) of  $x$  does  $f(x)$  attain a global minimum **on the interval**  $[-2, 2]$ ?

$x = -2$        $x = -1$        $x = 0$        $x = 1$        $x = 2$       NONE OF THESE

At which of the following value(s) of  $x$  does  $f(x)$  attain a global maximum **on the interval**  $[-2, 2]$ ?

$x = -2$        $x = -1$        $x = 0$        $x = 1$        $x = 2$       NONE OF THESE