

7.(12 points)

(a) Find $\frac{dy}{dx}$ given the equation $y^3 - xy = 2$.

(b) Is there a point, (x_0, y_0) , where the tangent to the curve is horizontal (i.e., parallel to the x -axis)? If so, find one. If not, explain why not.

(c) Show that the point $(3,2)$ lies on the curve, and find the equation of the tangent line to the curve at $(3,2)$.

(d) Use local linearization to find a good approximation for a value of y when the point $(3.09, y)$ lies on the curve. [Show your work.]