

3. (12 pts.) Some of the values of the functions  $f$ ,  $g$ ,  $f'$ ,  $g'$  are given in the following table.

$x$	$f(x)$	$g(x)$	$f'(x)$	$g'(x)$
0	1	1	5	$1/3$
1	3	-4	$-1/3$	$-8/3$

(a) If  $h(x) = g(f(x))$ , then  $h'(0) = \underline{-40/3}$ .

$$h'(x) = g'(f(x)) \cdot f'(x)$$

$$\begin{aligned} h'(0) &= g'(f(0)) \cdot f'(0) \\ &= g'(1) \cdot 5 \\ &= \left(-\frac{8}{3}\right)(5) = -\frac{40}{3} \end{aligned}$$

(b) If  $h(x) = \frac{f(x)}{g(x)+2}$ , then  $h'(1) = \underline{13/6}$ .

$$h'(x) = \frac{f'(x)(g(x)+2) - f(x)g'(x)}{(g(x)+2)^2}$$

$$\begin{aligned} h'(1) &= \frac{\left(-\frac{1}{3}\right)(-4+2) - (3)\left(-\frac{8}{3}\right)}{(-4+2)^2} = \frac{\left(\frac{2}{3}\right) + 8}{4} = \frac{\frac{26}{3}}{4} = \frac{26}{12} \\ &= \frac{13}{6} \end{aligned}$$

(c) If  $h(x) = \ln(f(x))$ , then  $h'(1) = \underline{-1/9}$ .

$$h'(x) = \frac{1}{f(x)} \cdot f'(x)$$

$$h'(1) = \frac{1}{3} \cdot \left(-\frac{1}{3}\right) = -\frac{1}{9}$$