

1. (2 points each) Circle “True” if the statement is *always* true. Otherwise, circle “False.” No explanation is necessary.

(a) Let  $f$  be a continuous function on the interval  $[1, 10]$  and differentiable on  $(1, 10)$ . Suppose that  $f(5) = 3$  and  $f(2) = 1$ . Then there is a point  $c$  in the interval  $(2, 5)$  so that  $f'(c) = \frac{2}{3}$ .

True                      False

(b) If  $g(x) = \frac{1}{f(x)}$ , then  $g'(x) = -\frac{1}{[f'(x)]^2}$ .

True                      False

(c) If  $a$  is a local maximum for the function  $f$  on the interval  $[2, 50]$ , then  $f'(a) = 0$ .

True                      False

(d) If  $g(x) = f^{-1}(x)$ , then  $g'(x) = (-1)f^{-2}(x)$ .

True                      False

(e) The 100<sup>th</sup> derivative of  $f(x) = x^5 + e^{2x}$  at  $x = 0$  is  $2^{100}$ .

True                      False

(f) If  $f(x) = (x-1)(x-2)(x-3)(x-4)(x-5)(x-6)$ , then  $f'(x) = (x-1) + (x-2) + (x-3) + (x-4) + (x-5) + (x-6)$ .

True                      False

(g) If  $f$  is continuous on  $[a, b]$ , then  $f$  has a global maximum and a global minimum on that interval.

True                      False