8. (10 points) The ideal gas law relates the volume and pressure of a gas to the temperature of the gas. The formula can be given as

$$
P V=c T
$$

where $P$ is the pressure of the gas measured in atmospheres, $V$ is the volume of the gas measured in liters, $c$ is a positive constant, and $T$ is the temperature of the gas measured in kelvins. (Remember, a temperature measured in kelvins is always positive!)
(a) If $T$ is held constant, find $\frac{d V}{d P}$.
(b) What is the meaning of the sign of your answer to part (a)? Explain this in everyday terms.
(c) Suppose $V, P$, and $T$ are all functions of the time $t$. Find $\frac{d T}{d t}$.

