

1. (8 points) The following table gives values of a continuous, differentiable function f' (i.e., the derivative of f). The statements below the table concern f . For each answer, give the smallest interval that is indicated by the table.

| | | | | | | | | | |
|---------|----|----|----|----|----|----|----|---|---|
| x | -4 | -3 | -2 | -1 | 0 | 1 | 2 | 3 | 4 |
| $f'(x)$ | 3 | 4 | 3 | 2 | -1 | -7 | -2 | 4 | 6 |

- (a) The function f has a local minimum between $x = \underline{\hspace{1cm}}$ and $x = \underline{\hspace{1cm}}$.
- (b) The function f has a local maximum between $x = \underline{\hspace{1cm}}$ and $x = \underline{\hspace{1cm}}$.
- (c) The function f has an inflection point between $x = \underline{\hspace{1cm}}$ and $x = \underline{\hspace{1cm}}$. (There is more than one possible answer here.)

2. (10 points) Let g be a function such that $g(2) = 4$ and whose derivative is known to be $g'(x) = \sqrt{x^2 + 2}$.

- (a) Use a linear approximation to estimate the value of $g(1.95)$. Show your work.
- (b) Do you think your estimate in part (a) is an overestimate or an underestimate? Explain.