

2. (11 points) Let  $f(x)$  be a **continuous** function defined for all real numbers  $x$ . Sketch a possible graph of  $f$ , given that

- $f(4) = 2$ ;
- $f'(x) > 0$  and  $f''(x) < 0$  for  $x < 2$ ;
- $f'(2) = 0$  and  $f''(2) = 0$ ;
- $f''(x) > 0$  for  $2 < x < 4$ ;
- $f''(4) = 0$ ;
- $f''(x) < 0$  for  $x > 4$ ;
- $f'(x) > 0$  for  $2 < x < 5$ ;
- $f'(5) = 0$ ;
- $f'(x) < 0$  for  $x > 5$ .

