1. (8 points) On the axes below are graphed $f, f^{\prime}$, and $f^{\prime \prime}$. Determine which is which, and justify your response with a brief explanation.


II: $\qquad$

III : $\qquad$

## Explanation:

The function $I I I$ achieves a minimum at $x=B$ (marked in the figure above); since neither $I$ nor $I I$ is 0 there, $I I I$ must be $f^{\prime \prime}$. This tells us that $f^{\prime \prime}$ is 0 at the point marked $A$ in the graph. Since the curve $I I$ achieves a minimum at $x=A$ while $I$ clearly has non-zero derivative there, $I I$ must be $f^{\prime}$. This in turn implies that $I$ must be $f$.
[Note: there are many answers for this part of the question.]

