

7. [10 points] For each real number  $k$ , there is a curve in the plane given by the equation

$$e^{y^2} = x^3 + k.$$

a. [4 points] Find  $\frac{dy}{dx}$ .

b. [3 points] Suppose that  $k = 9$ . There are two points on the curve where the tangent line is horizontal. Find the  $x$  and  $y$  coordinates of each one.

c. [3 points] Now suppose that  $k = \frac{1}{2}$ . How many points are there where the curve has a horizontal tangent line?