4. [8 points] A ship's captain is standing on the deck while sailing through stormy seas. The rough waters toss the ship about, causing it to rise and fall in a sinusoidal pattern. Suppose that t seconds into the storm, the height of the captain, in feet above sea level, is given by the function

$$h(t) = 15\cos\left(kt\right) + c$$

where k and c are nonzero constants.

a. [3 points] Find a formula for v(t), the vertical velocity of the captain, in feet per second, as a function of t. The constants k and c may appear in your answer.

Answer: v(t) = _____

b. [2 points] Find a formula for v'(t). The constants k and c may appear in your answer.

Answer: v'(t) = _____

c. [3 points] What is the maximum vertical acceleration experienced by the captain? The constants k and c may appear in your answer. You do not need to justify your answer or show work. Remember to include units.

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Answer: Max vertical acceleration: