

4. [10 points] Let $h(x)$ be a twice differentiable function defined for all real numbers x . (So h is differentiable and its derivative h' is also differentiable.)

Some values of $h'(x)$, the derivative of h are given in the table below.

x	-8	-6	-4	-2	0	2	4	6	8
$h'(x)$	3	7	0	-3	-5	-4	0	-2	6

For each of the following, circle all the correct answers.

Circle "NONE OF THESE" if none of the provided choices are correct.

- a. [2 points] Circle all the intervals below in which $h(x)$ must have a critical point.

$$-8 < x < -6 \quad -6 < x < -2 \quad -2 < x < 2 \quad 2 < x < 6 \quad 6 < x < 8$$

NONE OF THESE

- b. [2 points] Circle all the intervals below in which $h(x)$ must have a local extremum (i.e. a local maximum or a local minimum).

$$-8 < x < -6 \quad -6 < x < -2 \quad -2 < x < 2 \quad 2 < x < 6 \quad 6 < x < 8$$

NONE OF THESE

- c. [2 points] Circle all the intervals below in which $h(x)$ must have an inflection point.

$$-8 < x < -4 \quad -4 < x < 0 \quad 0 < x < 4 \quad 2 < x < 6 \quad 4 < x < 8$$

NONE OF THESE

- d. [2 points] Circle all the intervals below which must contain a number c such that $h''(c) = 2$.

$$-8 < x < -6 \quad -4 < x < -2 \quad -2 < x < 0 \quad 2 < x < 4 \quad 6 < x < 8$$

NONE OF THESE

- e. [2 points] Suppose that $h''(x) < 0$ for $x < -8$, and $h(-8) = 7$. Circle all the numbers below which could equal the value of $h(-10)$.

$$-2 \quad -1 \quad 0 \quad 1 \quad 2$$

NONE OF THESE