4. [10 points] Let $h(x)$ be a twice differentiable function defined for all real numbers $x$. (So $h$ is differentiable and its derivative $h^{\prime}$ is also differentiable.)
Some values of $h^{\prime}(x)$, the derivative of $h$ are given in the table below.

| $x$ | -8 | -6 | -4 | -2 | 0 | 2 | 4 | 6 | 8 |
| :---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| $h^{\prime}(x)$ | 3 | 7 | 0 | -3 | -5 | -4 | 0 | -2 | 6 |

For each of the following, circle all the correct answers.
Circle "none of these" if none of the provided choices are correct.
a. [2 points] Circle all the intervals below in which $h(x)$ must have a critical point.

$$
\begin{array}{lll}
-8<x<-6 & -6<x<-2 & -2<x<2 \\
\hline
\end{array}
$$

## NONE OF THESE

b. [2 points] Circle all the intervals below in which $h(x) \underline{\text { must }}$ have a local extremum (i.e. a local maximum or a local minimum).

$$
-8<x<-6 \quad-6<x<-2 \quad-2<x<2 \quad 2<x<6 \quad 6<x<8
$$

## NONE OF THESE

c. [2 points] Circle all the intervals below in which $h(x)$ must have an inflection point.

$$
\begin{array}{|lll|}
\hline-8<x<-4 & -4<x<0 & 0<x<4 \\
\hline
\end{array}
$$

## NONE OF THESE

d. [2 points] Circle all the intervals below which must contain a number $c$ such that $h^{\prime \prime}(c)=2$.

$$
\begin{array}{|llll}
-8<x<-6 & -4<x<-2 & -2<x<0 & 2<x<4
\end{array} 6<x<8
$$

NONE OF THESE
e. [2 points] Suppose that $h^{\prime \prime}(x)<0$ for $x<-8$, and $h(-8)=7$. Circle all the numbers below which could equal the value of $h(-10)$.
$-2$
$-1$
0
1
2

