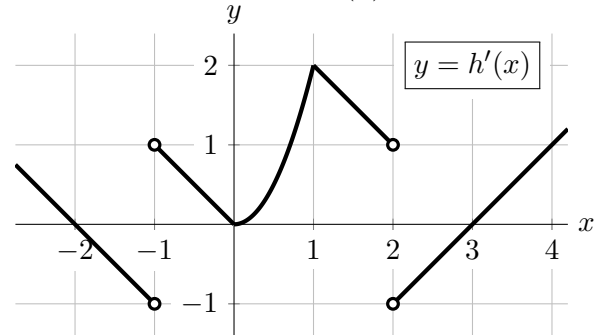


3. [14 points] A table of values for a differentiable, invertible function  $g(x)$  and its derivative  $g'(x)$  are shown below to the left. (This is the same table as in the previous problem.) Below to the right is shown a portion of the graph of  $h'(x)$ , the **derivative** of a function  $h(x)$ . The function  $h(x)$  is defined and continuous for all real numbers.

|         |     |     |     |     |     |   |
|---------|-----|-----|-----|-----|-----|---|
| $x$     | 0   | 1   | 2   | 3   | 4   | 5 |
| $g(x)$  | 0   | 0.5 | 1   | 2   | 5   | 6 |
| $g'(x)$ | 1.9 | 1.5 | 2.8 | 2.5 | 2.6 | 3 |



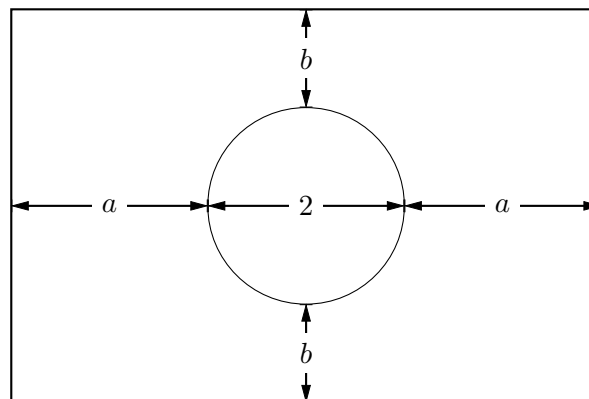
Answer parts **a.–c.**, or write NONE if appropriate. You do not need to show work.

- [2 points] List the  $x$ -coordinates of all critical points of  $h(x)$  on the interval  $(-2, 4)$ .
- [2 points] List the  $x$ -coordinates of all critical points of  $h'(x)$  on the interval  $(-2, 4)$ .
- [2 points] List the  $x$ -coordinates of all local minima of  $h(x)$  on the interval  $(-2, 4)$ .
- [8 points] A curve is described implicitly by the equation

$$yg(x) = e^{h(x)}.$$

Assume  $h(1) = 0$ . Then the point  $(1, 2)$  lies on this curve.

- Find  $\frac{dy}{dx}$  at the point  $(1, 2)$ . You must show every step of your work.
  - Write an equation for the tangent line to the curve at the point  $(1, 2)$ .
4. [10 points] A landscaper is designing a rectangular garden surrounding a circular fountain in the middle.
- The diameter of the fountain is 2 meters.
  - The distance from the fountain to the eastern and western edges of the garden is  $a$  meters.
  - The distance from the fountain to the northern and southern edges of the garden is  $b$  meters.
  - The part of the garden **outside of the circular fountain** will be covered with exactly 300 square meters of grass.



- [4 points] Write a formula for  $b$  in terms of  $a$ .
- [2 points] Write a formula for the function  $P(a)$  which gives the rectangular perimeter of the garden in terms of  $a$  only.