4. [8 points]

Sunny and Tyrell own an ice cream shop together. They want to sell waffle cones in the usual shape of a cone, as shown on the right. The cost, in dollars, of a waffle cone with radius $r$ inches and height $h$ inches is

$$
\frac{r}{2}\left(\sqrt{h^{2}+r^{2}}\right) .
$$

Sunny and Tyrell want to spend exactly $\$ 5$ on a waffle cone that can fit the most ice cream (i.e has the largest volume).
Note that the volume of a cone of radius $r$ and height $h$ is $\frac{\pi r^{2} h}{3}$.
a. [3 points] Write a formula for $h$ in terms of $r$ if the cone costs $\$ 5$.

Answer: $h=$ $\qquad$
b. [2 points] Write a formula for the function $V(r)$ which gives the volume, in cubic inches, of an ice cream cone that costs $\$ 5$ in terms of $r$ only. Your formula should not include the letter $h$.

Answer: $\quad V(r)=$ $\qquad$
c. [3 points] What is the domain of $V(r)$ in the context of this problem?

