(10.) (11 points) You are designing a cylindrical bucket. The bucket must have a bottom, but it will have no lid, and you have 1000 square inches of steel sheet to use for the bucket.
If the radius of the bucket is $r$ and the height is $h$, for what values of $r$ and $h$ does the bucket have maximum possible volume? What is this maximum volume? Show all your work, and clearly indicate your final answers below.

Optimal value of $r=$ $\qquad$

Optimal value of $h=$ $\qquad$

Maximum volume $=$ $\qquad$

