## MATH 115 - FINAL EXAM SOLUTIONS

1. (12 points) Let $g(x)$ be a continuous function such that $\int_{2}^{3} g(x) d x=5$. Let $f(x)$ be given by the following graph:

(a) Find $f^{\prime}(1)$.
$f^{\prime}(1)=2$.
(b) Find $\int_{1}^{2} g(x+1) d x$.
$\int_{1}^{2} g(x+1) d x=5$.
(c) Find the average value of $f$ on the interval $[0,4]$.

The average value of $f$ over $[0,4]=3$.
(d) Find $\int_{2}^{3}(f(x)+3 g(x)) d x$.
$\int_{2}^{3}(f(x)+3 g(x)) d x=19$.
(e) If $G^{\prime}(x)=g(x)$ and $G(2)=7$, find $G(3)$.
$G(3)=12$.
(f) If $F^{\prime}(x)=f(x)$, describe two graphical features of $F$ on the interval $0<x<1$.
$F$ is increasing and concave up.

