

2. (4 points each) Suppose that f , g and h are continuous and differentiable functions such that $f'(x) = g(x)$ and **ALL** of the following conditions are also true:

$$\int_0^5 f(x)dx = -2, \quad \int_5^{10} g(x)dx = 2, \quad \int_0^5 g(x)dx = 15,$$

$$f(0) = 7, \quad h(x) = g(x - 5)$$

For parts (a)-(f), find the numerical value indicated. If insufficient information is given to answer the question indicate “Insufficient information”.

$$(a) \int_0^5 f(0)g(x)dx = f(0) \int_0^5 g(x)dx = 7(15) = 105$$

$$(b) f(10) = \int_0^{10} g(x)dx + f(0) = \int_0^5 g(x)dx + \int_5^{10} g(x)dx + f(0) = 15 + 2 + 7 = 24$$

$$(c) \int_0^5 |f(x)| dx = \text{Insufficient Information}$$

$$(d) \int_0^5 \left(3f(0) - \frac{g(x)}{5} \right) dx = 3f(0) \int_0^5 dx - \frac{1}{5} \int_0^5 g(x)dx = 3(7)(5) - \frac{1}{5}(15) = 102$$

$$(e) \int_0^5 \frac{1}{g(x)} dx = \text{Insufficient Information}$$

$$(f) \int_5^{10} h(x)dx = \int_0^5 g(x)dx = 15$$