

4. (12 points) Suppose that  $f$ ,  $g$  and  $h$  are all continuous and differentiable functions such that:

- $f$  is an odd function
- $\int_0^3 f(t) dt = 3$
- $g(t) = t^2 + 2$
- $h(t) = g'(t - 1)$

Evaluate the following, where possible. If evaluation is not possible, simply state “insufficient information.”

(a)  $\int_{a+3}^{a+3} f(t) dt = 0$

(b)  $\int_{-10}^{10} f(t) dt = 0$       (since  $f$  is odd)

(c) The average value of  $g$  on the interval  $[-2, 2]$

$$\frac{1}{4} \int_{-2}^2 (t^2 + 2) dt = \frac{1}{4} \left( \frac{t^3}{3} + 2t \right) \Big|_{-2}^2 = \frac{10}{3}$$

(d)  $\int_{-3}^0 f(t) dt = -3$

(e)  $\int_{-1}^1 h(t) dt = g(0) - g(-2) = 2 - (4 + 2) = -4$