

2. [6 points] For each of the following statements, circle TRUE if the statement is always true and circle FALSE otherwise. Any ambiguous answers will be marked as incorrect.

- a. [2 points] Suppose  $A(t)$  and  $B(t)$  are both everywhere differentiable functions which satisfy the equation  $A^2 = e^B$  for all real numbers  $t$ . If, additionally,  $\ln(2A(0)) = B(0)$ , then  $A'(0) = B'(0)$ .

True                  False

- b. [2 points] If  $f(x)$  is an everywhere continuous function and  $\int_1^b f(t-b)dt = c$  for some real numbers  $b$  and  $c$ , then  $\int_0^{1-b} 5f(t)dt = -5c$ .

True                  False

- c. [2 points] If  $r(y)$  is a twice differentiable function whose first derivative is continuous, decreasing, and negative for all real numbers  $y$ , then  $r(y)$  is concave up.

True                  False