4. [14 points] Consider the family of functions

$$y = x^{2b} + ax^b$$

where a and b are nonzero constants.

a. [4 points] Calculate y'.

b. [4 points] Calculate y''.

c. [6 points] Find values of a and b so that the resulting function has an inflection point at (x,y)=(1,-4). Justify that (1,-4) is an inflection point of the function with the values of a and b that you found.