4. [14 points] Consider the family of functions

$$
y=x^{2 b}+a x^{b}
$$

where $a$ and $b$ are nonzero constants.
a. [4 points] Calculate $y^{\prime}$.
b. [4 points] Calculate $y^{\prime \prime}$.
c. [6 points] Find values of $a$ and $b$ so that the resulting function has an inflection point at $(x, y)=(1,-4)$. Justify that $(1,-4)$ is an inflection point of the function with the values of $a$ and $b$ that you found.

