

7. [11 points] Consider the continuous function

$$f(x) = \begin{cases} x \cdot 2^{-x} & 1 \leq x < 3, \\ \frac{1}{2-x} + \frac{11}{8} & 3 \leq x \leq 5. \end{cases}$$

Note that the domain of  $f$  is  $[1, 5]$ .

a. [7 points] Find the  $x$ -values of the critical points of  $f$ .

b. [4 points] Find the  $y$ -values of the global maximum and global minimum of  $f$  if they exist, or explain why they don't exist.