1. [13 points]

The graph of a function h(x) is shown on the right. The area of the shaded region A is 4, and h(x) is piecewise linear for $3 \le x \le 6$.

Compute each of the following. If there is not enough information to compute a value exactly, write NOT ENOUGH INFO.

a. [2 points] Find
$$\int_{0}^{3} (h(x) + 2) dx$$
.

Answer:
$$\int_{0}^{3} (h(x) + 2) dx = 1$$

b. [2 points] Find the average value of h(x) on the interval [0, 4].

Answer:

c. [3 points] Let $J(x) = \sin(\pi h(x))$. Find J'(3.5).

Answer: J'(3.5) = _____

d. [3 points] Let H(x) be an antiderivative of h(x) with H(4) = 5. Find an equation for the tangent line to the graph of H(x) at x = 4.

Answer:
e. [3 points] Let
$$g(x) = e^x$$
. Find $\int_6^7 (g(x)h'(x) + g'(x)h(x)) dx$.

Answer:
$$\int_{6}^{7} \left(g(x)h'(x) + g'(x)h(x) \right) \, dx =$$

University of Michigan Department of Mathematics

