

11. [8 points] You are not required to show your work on this page.

- a. [2 points] A function  $f(x)$  is differentiable. Some values of  $f$  and  $f'$  are shown in the table below.

$x$	0	1	2	3	4
$f(x)$	3	4	1	-1	-2
$f'(x)$	2	-2	-3	0	3

Let  $g(x) = \cos(\frac{\pi}{2}f(x))$ . Which of the following values of  $x$  must be a critical point of  $g(x)$ ? Circle all such values.

0            1            2            3            4            NONE OF THESE

- b. [2 points] Which of the following expressions gives the linear approximation for  $\arctan(x)$  near  $x = 1$ ? Circle all such expressions.

- i.  $\frac{\pi}{4} + \frac{1}{2}(x - 1)$                       iii.  $\frac{1}{1+x^2} + \frac{\pi}{4}(x - 1)$                       v. NONE OF THESE  
 ii.  $\frac{1}{2} + \frac{\pi}{4}(x - 1)$                       iv.  $\arctan(x) + \frac{1}{2}(x - 1)$

- c. [2 points] Which of the following functions are antiderivatives of  $f(x) = \frac{1}{x}$ ? Circle all such functions.

- i.  $\ln(|x + 1|)$                       iii.  $\ln(|x|) + 2$                       v.  $4 \ln(|x|)$   
 ii.  $\ln(|x|)$                       iv.  $\ln(4|x|)$                       vi. NONE OF THESE

- d. [2 points] Suppose  $n$  is a positive integer,  $f$  is a decreasing, continuous function on the interval  $[2, 6]$ , the value of the left Riemann sum with  $n$  equal subdivisions for  $\int_2^6 f(x)dx$  is  $A$ , and  $f(2) = f(6) + 8$ . Circle all the statements that must be true.

- i.  $A$  is an overestimate for  $\int_2^6 f(x)dx$ .  
 ii.  $\int_2^6 f(x) dx = 8$ .  
 iii.  $\int_1^5 f(x + 1) dx = \int_2^6 f(x) dx$ .  
 iv. The left Riemann sum for  $\int_2^6 (f(x))^2 dx$  with  $n$  equal subdivisions is equal to  $A^2$ .  
 v. NONE OF THESE