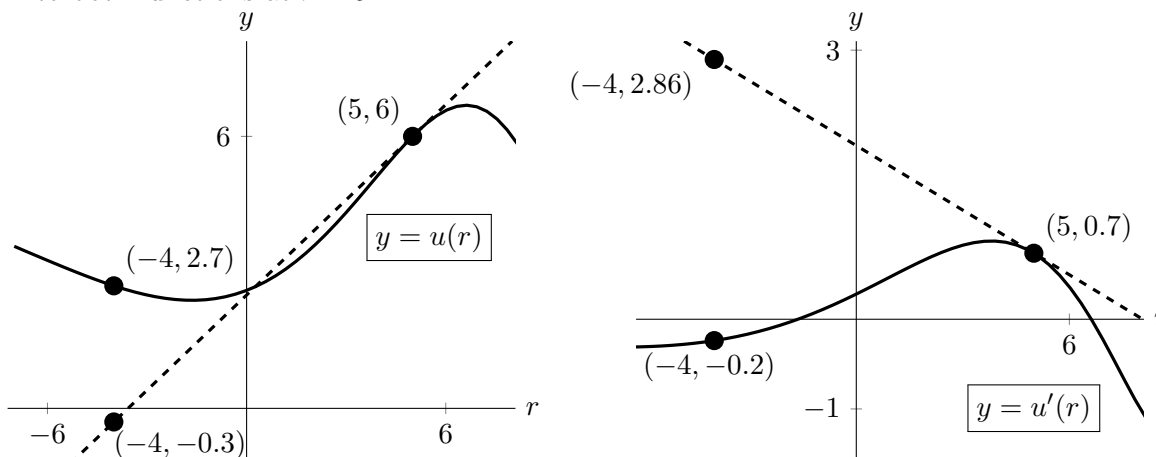


9. [9 points] The graphs of  $u(r)$  and  $u'(r)$  are shown below. The graphs also show tangent lines to both functions at  $r = 5$ .



The table below shows some values of  $h(s)$  and  $h'(s)$ . Both  $h$  and  $h'$  are differentiable.

$s$	-6	-4	-2	0	2	4	6
$h(s)$	1	4	5	-1	-3	4	7
$h'(s)$	3	2	-4	-1	0	2	1

- a. [5 points] Let  $g(t) = u(h(t))$ . Find a formula for  $\ell(t)$ , the local linearization of  $g(t)$  near  $t = -2$ , and use this to approximate a solution to  $g(t) = 6.14$ .

**Answer:**  $\ell(t) =$  \_\_\_\_\_

**Answer:**  $g(t) = 6.14$  when  $t \approx$  \_\_\_\_\_

- b. [2 points] Write a formula for  $c(r)$ , the quadratic approximation of  $u(r)$  at  $r = 5$ . (Recall that a formula for the quadratic approximation  $Q(x)$  of a function  $f(x)$  at  $x = a$  is  $Q(x) = f(a) + f'(a)(x - a) + \frac{f''(a)}{2}(x - a)^2$ .)

**Answer:**  $c(r) =$  \_\_\_\_\_

- c. [2 points] Use the data provided to estimate  $h''(-5)$ .

**Answer:**  $h''(-5) \approx$  \_\_\_\_\_