

1. [9 points] A portion of the graph of a function f is shown below.

Throughout this problem, you do not need to explain your reasoning.

For each of parts **a**.– **d**. below, circle all of the listed values satisfying the given statement. If there are no such values, circle NONE.

a. [2 points] For which of the following values of c is $\lim_{x \to c^-} f(x) = f(c)$?

- $c = -1 \qquad c = 0 \qquad c = 1$ c = -3c = 2.5NONE
- **b.** [2 points] For which of the following values of c is f(x) continuous at x = c?

$$c = -3$$
 $c = -1$ $c = 0$ $c = 1$ $c = 2.5$ None

c. [2 points] For which of the following values of c does f(x) appear to be differentiable at x = c?

c = -3 c = -1 c = 0 c = 1 c = 2.5NONE

- d. [3 points] Consider the quantities defined as follows:
 - III. $\int_{-1}^{1} f(x) dx$. II. f(1). I. The number 0.

IV. The left-hand Riemann sum with 2 equal subintervals for $\int_{-1}^{1} f(x) dx$.

V. The right-hand Riemann sum with 2 equal subintervals for $\int_{-1}^{1} f(x) dx$.

Rank the quantities in order from least to greatest by filling in the blanks below with the options I–V. You do not need to show your work.

I < III < IV < II < V

Fall, 2016 Math 115 Exam 3 Problem 1 Solution