3. [14 points] Suppose $f(x)$ is an even function. A piece of the graph of $f(x)$ is given below. Note that $f(x)$ is piecewise linear for $0 \leq x \leq 6$.
Find the following quantities. If any of their values do not exist, write DNE. If there is not enough information to answer, write NI.
a. [1 point] Find $\lim _{p \rightarrow 4^{+}} f(p)$.

## Answer:

$\qquad$

b. [2 points] Find $\lim _{m \rightarrow 0} \frac{f(1+m)-f(1)}{m}$.
c. [3 points] Let $g(x)=\frac{1}{\sqrt{4+f(2 x)}}$. Find $g^{\prime}(2.5)$.

Answer: $\qquad$

Answer: $\qquad$
d. [3 points] Recall that $f(x)$ is even. Find $\int_{-3}^{1}(5 f(t)-3) d t$.

Answer: $\qquad$
e. [3 points] Let $j(x)$ be an antiderivative of $f(x)$ with $j(5)=3$. Suppose that $p(x)$ is the quadratic approximation of $j(x)$ near $x=5$. Find a formula for $p(x)$.

Answer: $p(x)=$ $\qquad$
f. [2 points] Find all the values of $a$ with $-3 \leq a \leq 3$ such that $\int_{-2}^{a} f(x) d x=0$.
$\qquad$

