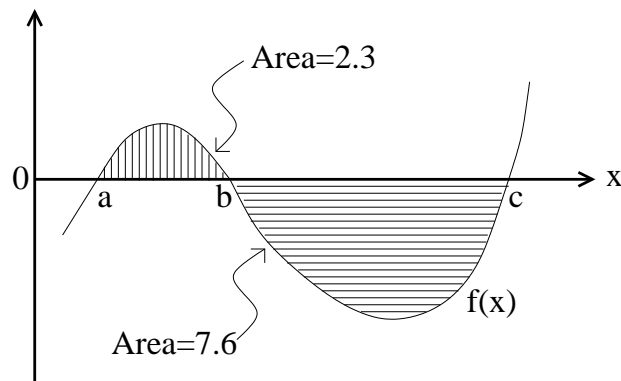
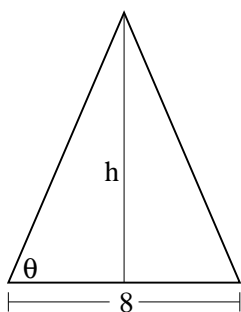


6. (8 points) Use the figure below to calculate the numerical values of the definite integrals in parts (a) through (d). You need not show your reasoning.



- (a) $\int_a^b f(x) dx = \underline{\quad 2.3 \quad}$
- (b) $\int_b^c f(x) dx = \underline{\quad -7.6 \quad}$
- (c) $\int_a^c f(x) dx = \underline{\quad -5.3 \quad}$
- (d) $\int_b^a f(x) dx = \underline{\quad -2.3 \quad}$

7. (8 points) An isosceles triangle has a base of length 8 meters. If θ denotes the angle opposite one of the two equal sides, and if θ is increasing at a constant rate of 0.1 radians per second, how fast is the area of the triangle increasing when $\theta = \pi/6$?



Solution: If $A(\theta)$ is the area of the triangle with angle θ , then we are asked to find the rate of change of A with respect to time when $\theta = \pi/6$. We are given that $d\theta/dt = .1$ radians per second.

Let h denote the height of the triangle. Since the triangle is isosceles, the perpendicular bisector of the base passes through the top vertex so $\tan \theta = h/(\text{half of base}) = h/4$ or $h = 4 \tan \theta$. Thus, the area A of the triangle is

$$A = \frac{1}{2} \text{base} \cdot \text{height} = \frac{1}{2}(8) \cdot (4 \tan \theta) = 16 \tan \theta \text{ square meters.}$$

From the chain rule and the formula for the derivative of the tangent function, we find $dA/dt = (16/\cos^2 \theta) d\theta/dt$. When $\theta = \pi/6$, $\cos \theta = \sqrt{3}/2$ so at this time,

$$\frac{dA}{dt} = \frac{16}{(\sqrt{3}/2)^2} \frac{d\theta}{dt} = \frac{64}{3} (.1) = \frac{6.4}{3} \simeq 2.1333 \text{ square meters per second.}$$