7. [10 points] Airwatt Construction company builds large-scale farms of wind turbines. A graph of cost C and revenue R for the company at different production levels q is shown below. Here cost and revenue are measured in billions of dollars and production level is measured in thousands of wind farms. In each of the following parts, be sure it is clear how you obtain your answers.



a. [3 points] Approximate the marginal revenue at q = 0.8. Show how you obtain your estimate.

Solution: The marginal revenue is the slope of the tangent line to the revenue curve. At q = 0.8 the slope is approximately 0.25/0.2 = 1.25. This means the marginal revenue is 1.25 billion dollars per thousand wind farms. Or if we reduce the units, it's \$1,250,000 per wind farm.

b. [3 points] Approximate the cost of producing one additional wind farm when q = 1.6.

Solution: The marginal cost is the slope of the tangent line to the cost curve. At q = 1.6 the slope is approximately 1. This means the marginal cost is 1 billion dollars per thousand wind farms. Reducing units, the cost to produce an additional wind farm when q = 1.6 is about \$1 million.

c. [4 points] Approximate the maximum profit which can be achieved by Airwatt. At what production level does this occur?

Solution: The maximum profit occurs at a point where the revenue curve is above the cost curve and MR=MC. This means the slopes of the tangent lines to the curves C and R are equal at the production level q in question. Looking on the graph, it appears this occurs somewhere between q = 1.5 and q = 1.7, say q = 1.6. The vertical distance between C and R at this point is about 0.3. So the maximum profit is about \$300 million and it occurs when 1600 wind farms have been built.