

5. [15 points] The function  $h(x)$  is not known, but the *derivative* of  $h(x)$  is given by the formula

$$h'(x) = \sin(x)e^{x^2+1}.$$

- a. [2 points] Find a formula for  $h''(x)$ .
- b. [6 points] List all critical points for  $h(x)$  in the open interval  $-2\pi < x < 2\pi$ . For each point, use an appropriate test to determine whether it is a local maximum, local minimum, or neither.
- c. [2 points] For which  $x$ -value in the closed interval  $\frac{\pi}{4} \leq x \leq \frac{\pi}{2}$  does  $h(x)$  attain its maximum value? (Do not try to find the  $y$ -coordinate.)
- d. [5 points] Write out all terms for a right-hand Riemann sum with three subintervals which approximates

$$\int_0^1 \sin(x)e^{x^2+1} dx.$$