

9. [8 points] Suppose  $g$  is a twice differentiable function with continuous second derivative. Several values of the first and second derivatives of  $g$  are shown in the table below.

$t$	-8	-6	-4	-2	0	2	4	6	8
$g'(t)$	-11	-10	-8	0	9	16	17	14	7
$g''(t)$	1	0	2	5	4	2	0	-2	-4

Assume that between each pair of consecutive values of  $t$  shown in the table, each of  $g'(t)$  and  $g''(t)$  is either always strictly decreasing or always strictly increasing.

- a. [2 points] Use the local linearization of  $g'(t)$  near  $t = 6$  to estimate  $g'(5.8)$ .

**Answer:**  $g'(5.8) \approx$  \_\_\_\_\_

- b. [1 point] Indicate whether the local linearization of  $g'(t)$  near  $t = 6$  gives an overestimate or an underestimate of the value of  $g'(5.8)$ . If there is not enough information to make this determination, circle “not enough information”. You do not need to explain.

**Answer:** This estimate is an (circle one):

overestimate          underestimate          not enough information

- c. [5 points] Let  $f$  be the quadratic function defined by  $f(t) = t^2 - 4t + 6$ . and let  $R$  be the function defined by  $R(t) = f(t) - g(t)$ . At what, if any, values of  $t$  does  $R'(t)$  (the derivative of  $R(t)$ ) attain its global extrema in the open interval  $-8 < t < 8$ ?

For each answer blank, write NONE if  $R'(t)$  does not attain a global extremum of that type on the open interval  $-8 < t < 8$ , and write NOT ENOUGH INFO if the  $t$  value(s) cannot be determined exactly. Use calculus to find and justify your answers, and be sure to show enough evidence to demonstrate that you have found where the global extrema occur.

**Answer:** Global min(s) at  $t =$  \_\_\_\_\_ and Global max(es) at  $t =$  \_\_\_\_\_