6. [14 points] A portion of the graph of a function p(x) is shown below. The area of the shaded region is 8, and the portion of the graph on the interval [-3,0] is a quarter circle. Also note that p(x) is linear on the intervals (0,2) and (4,5).



Let P(x) be the continuous antiderivative of p(x) passing through the point (0, 1).

- a. [3 points] Find all critical points of P(x) in the interval (-7, 5). For each, determine if it a local maximum, local minimum, or neither.
- **b.** [2 points] For what values of x in the interval (-7, 5) is P(x) a linear function? Give your answer as one or more intervals.
- c. [2 points] For approximately what values of x in the interval (-7,5) is the function P(x) concave up? Give your answer as one or more intervals.
- **d**. [2 points] For approximately what values of x in the interval (-7, 5) is the function p''(x) positive? Give your answer as one or more intervals.
- e. [5 points] Create a table giving the exact values of P(x) at x = -7, -3, 0, 2, 4, and 5.