6. [14 points] A portion of the graph of a function $p(x)$ is shown below. The area of the shaded region is 8, and the portion of the graph on the interval $[-3, 0]$ is a quarter circle. Also note that $p(x)$ is linear on the intervals $(0, 2)$ and $(4, 5)$.

Let $P(x)$ be the continuous antiderivative of $p(x)$ passing through the point $(0, 1)$.

**a.** [3 points] Find all critical points of $P(x)$ in the interval $(-7, 5)$. For each, determine if it a local maximum, local minimum, or neither.

**b.** [2 points] For what values of $x$ in the interval $(-7, 5)$ is $P(x)$ a linear function? Give your answer as one or more intervals.

**c.** [2 points] For approximately what values of $x$ in the interval $(-7, 5)$ is the function $P(x)$ concave up? Give your answer as one or more intervals.

**d.** [2 points] For approximately what values of $x$ in the interval $(-7, 5)$ is the function $p''(x)$ positive? Give your answer as one or more intervals.

**e.** [5 points] Create a table giving the exact values of $P(x)$ at $x = -7, -3, 0, 2, 4,$ and $5$. 

![Graph of a function with shaded region and labeled points](image-url)