

1. (7 points) The *sine-integral* function  $Si(x)$  is defined by

$$Si(x) = \int_0^x \frac{\sin t}{t} dt.$$

What is the derivative of  $Si(x^3)$ ?

Answer:  $\frac{d}{dx}Si(x^3) =$  \_\_\_\_\_

2. (10 points) Let  $g(x)$  be a continuously differentiable functions of  $x$  that satisfies  $g(1) = 2$ ,  $g(5) = 6$ , and  $\int_1^5 g(x) dx = -2$ . Compute, showing all your work,

(a)  $\int_1^5 xg'(x)dx =$  \_\_\_\_\_ .

(b)  $\int_2^3 g(4x - 7) dx =$  \_\_\_\_\_

3. (6 points) Let  $r(t)$  represent the rate that the height of a child changes per year (in inches per year), where  $t = 0$  corresponds to the birth date of the child. Explain the meaning of the quantity  $\int_4^8 r(t) dt$ . (Remember to use units.)