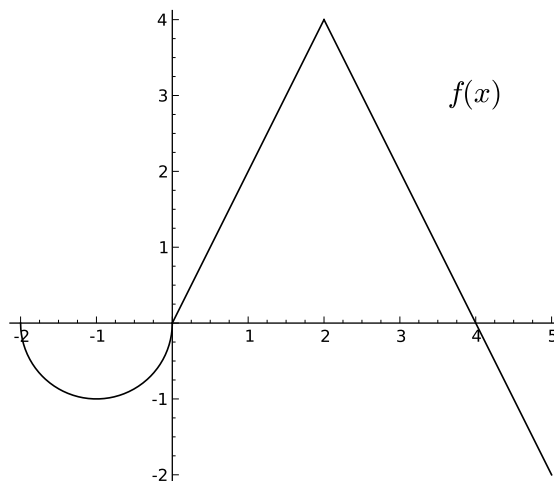


2. [18 points] The graph of the function  $f(x)$ , shown below, consists of line segments and a semicircle. Compute each of the following quantities.



a. [7 points]

1.  $\int_0^2 f(x) dx = 4.$

2.  $\int_{-2}^2 |f(x)| dx = \frac{\pi}{2} + 4 \approx 5.57.$

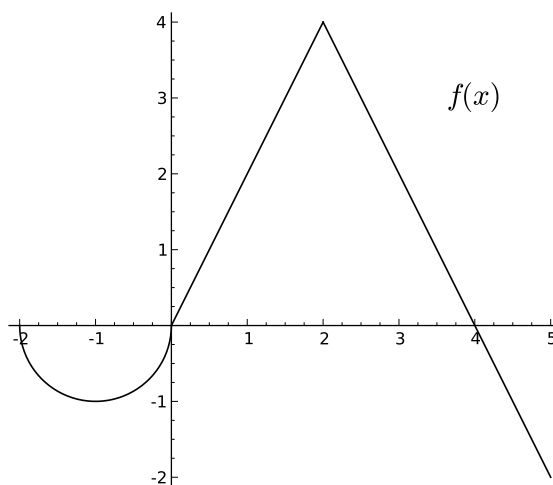
3.  $\int_0^5 f(x) dx = 8 - 1 = 7.$

4.  $\int_{-2}^2 2f(x) dx + \int_5^2 3f(x) dx = 2(4 - \frac{\pi}{2}) - 3(4 - 1) = -1 - \pi \approx -4.14.$

5. The average  $A$  of  $f(x)$  on the interval  $[-2, 5]$ .  $A = \frac{1}{7} \int_{-2}^5 f(x) dx = \frac{7 - \frac{\pi}{2}}{7} \approx .775.$

6.  $\int_0^1 f(5x) dx = \frac{1}{5} \int_0^5 f(u) du = \frac{7}{5}.$

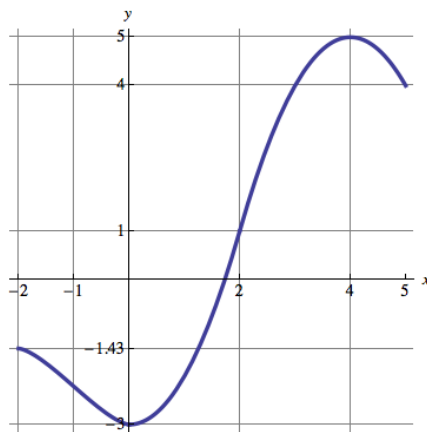
b. [4 points]



If  $f(x)$  is the derivative of a function  $g(x)$  with  $g(2) = 1$ , fill in the table of values of  $g(x)$ , provided below, at the specified points (the graph has been reproduced for your convenience):

$x$	-2	0	2	4	5
$g(x)$	$\frac{\pi}{2} - 3 \approx -1.429$	-3	1	5	4

c. [5 points] Graph  $g(x)$ . Make sure your graph indicates the intervals on which  $g(x)$  is increasing, decreasing, concave up, and concave down.



d. [2 points] Let  $h(x) = \int_0^x f(t) dt$ . Find a constant  $C$  such that  $g(x) = h(x) + C$ . Show all your work.

$$g(x) = 1 + \int_2^x f(t) dt = 1 + \int_0^x f(t) dt - \int_0^2 f(t) dt = 1 + h(x) - 4$$

$$g(x) = h(x) - 3.$$

$$C = -3.$$