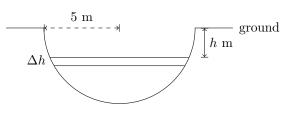
8. [12 points]

Alicia is building a pond in her backyard. The pond will be in the shape of hemisphere with radius 5 meters. A side view of the hole for the pond is shown in the figure on the right. Note: The curved region shown is a semicircle of radius 5 meters, and cross-sections of the hole parallel to the ground are circles.



Alicia discovers that the density (in kg/m³) of the dirt in her yard is given by the function $\rho(h) = 1.5 + (h-1)^3$ where h is distance (in meters) below ground. In this problem, you may assume the acceleration due to gravity is $g = 9.8 \text{ m/s}^2$.

a. [4 points] Write an expression that gives the approximate mass of a horizontal slice of dirt with thickness Δh meters that is h meters below the ground. See diagram. (Assume that Δh is small but positive.) Your expression should <u>not</u> involve any integrals.

Answer: Mass of slice \approx

b. [3 points] Write, but do <u>not</u> evaluate, an expression involving one or more integrals that gives the mass (in kg) of the dirt Alicia removes in order to create the hole for her pond.

Answer: $Mass = _$

c. [5 points] As Alicia digs, she lifts the dirt 1 meter above the ground to put it into the back of a truck. Write, but do <u>not</u> evaluate, an expression involving one or more integrals that gives the work Alicia does to remove all the dirt from the hole for her pond.

Answer: Work =

(include units)