5. [15 points] Consider the region R in the xy-plane bounded between $y = \cos(x)$ and y = -1 for x values between $-\pi$ and π . A sketch of the region is shown below.



a. [5 points] Find an expression involving one or more integrals for the volume of the solid formed by rotating the region R around the line x = 5. Do not evaluate your integral(s).

b. [5 points] Find an expression involving one or more integrals for the volume of the solid formed by rotating the region R around the line y = -3. Do not evaluate your integral(s).

c. [5 points] Find an expression involving one or more integrals for the volume of the solid with a base in the shape of the region R, and semicircular cross sections perpendicular to the x-axis. Do not evaluate your integral(s).