3. [9 points] Anna and Burt have come to an agreement after Labor Day's food debacle. They've decided to cook lasagna for their family's next get-together. They practice cooking the lasagna over the course of 4 hours. Let L(t) be the tastiness of the lasagna, measured in tasty units, t hours after they begin cooking. L(t) is given by

$$L(t) = \int_{1}^{t^{2} - 3t + 3} \frac{7}{1 + x^{4}} dx + 3, \text{ for } 0 \le t \le 4.$$

a. [2 points] There are exactly two times within the interval [0, 4] where the lasagna is 3 tasty units. What are those times? Show your work.

Answer:

b. [4 points] During what interval(s) in [0,4] is the lasagna's tastiness decreasing? Justify your answer(s) using calculus.

Answer:

c. [3 points] Find a function f(x) and constants a and C so that we may rewrite L(t) in the form

$$L(t) = \int_{0}^{t} f(x) \, \mathrm{d}x + C.$$

There may be more than one correct answer.

$$f(x) =$$

$$a =$$

$$C = \underline{\hspace{1cm}}$$