6. [15 points] The curves $x = y^2 - 4y + 5$ and $x = 5 + 2y - y^2$ intersect at the points (2,3) and (5,0), as seen in the diagram below. Consider the region, R, bounded by the two curves.



a. [5 points] Find an expression involving one or more integrals for the volume of the solid formed by rotating the region R around the line x = 0 (i.e. the y-axis). Do not evaluate your integral(s).

Answer:

b. [5 points] Find an expression involving one or more integrals for the volume of the solid formed by rotating the region R around the line y = 4. Do not evaluate your integral(s).

Answer:

c. [5 points] Find an expression involving one or more integrals for the volume of the solid which has the region R as its base, and which has square cross-sections perpendicular to the y-axis. Do not evaluate your integral(s).