

1. (3 pts each) Circle true or false. No explanation necessary.

(a) If  $0 < f(x) < g(x)$  for all  $x$ , then  $\int_1^4 \frac{g(x)}{f(x)} dx > 3$ .

True  $\int_1^4 \frac{g(x)}{f(x)} dx > \int_1^4 \frac{f(x)}{f(x)} dx = \int_1^4 1 dx = x \Big|_1^4 = 4 - 1 = 3.$

(b)  $\int_{\pi}^{\pi} \frac{\sin^2(x^5) - \cos(42x)}{x^2 + x + 1} dx > 2$ .

False The integral is from  $\pi$  to  $\pi$ , so it's 0.

(c)  $\int_1^{\infty} \frac{1}{x^{71}} dx$  converges.

True  $\int_1^{\infty} \frac{1}{x^{71}} dx = \lim_{b \rightarrow \infty} \int_1^b x^{-71} dx = \lim_{b \rightarrow \infty} -\frac{1}{70} x^{-70} \Big|_1^b = \lim_{b \rightarrow \infty} -\frac{1}{70b^{70}} + \frac{1}{70} = \frac{1}{70}.$

(d) If  $g(x) + 2$  is an antiderivative of  $f(x)$ , then  $g(x)$  is also an antiderivative of  $f(x)$ .

True  $g(x) + 2$  and  $g(x)$  have the same derivative.

2. (6 pts) State the construction theorem for antiderivatives.

If  $f(x)$  is continuous on the closed interval  $[a, b]$ , then the function  $F(x) = \int_a^x f(t) dt$  is an antiderivative of  $f(x)$  for  $a \leq x \leq b$ .