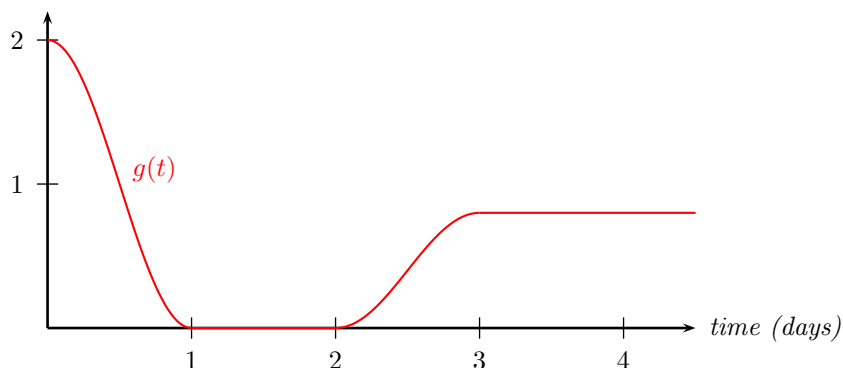


9. (14 pts) In springtime, as a nameless old tree quietly builds its leaves and branches by drawing matter out of the air and earth, an unnamed old botanist measures the process with care:

Rate of new growth (kg/day)



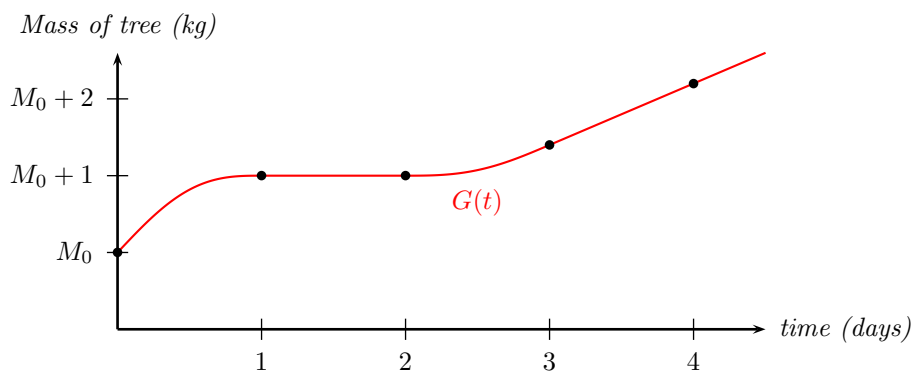
- (a) (2 pts) Estimate  $\int_0^4 g(t) dt$ .

$$\text{TRAP}(4) = 1 \left( \frac{1}{2}g(0) + g(1) + g(2) + g(3) + \frac{1}{2}g(4) \right) = \frac{1}{2}(2) + 0 + 0 + .8 + \frac{1}{2}(.8) = \boxed{2.2}.$$

- (b) (4 pts) Explain what your answer to part (a) tells you about the tree.

The tree grew about 2.2 kg in the four days between time 0 and time 4.

- (c) (6 pts) Sketch a possible graph of the mass of the tree as a function of time during this particular season. Label your graph carefully.



Here  $M_0$  is the initial mass of the tree.

- (d) (2 pts) What can you say about the derivative of the function you sketched in part (c)?

The derivative of  $G(t)$  is  $g(t)$ .