

6. (20 points) The quantity $\int_1^{\infty} \frac{dx}{\sqrt{(a^2+x)(b^2+x)(c^2+x)}}$ roughly models the resistance that football-shaped plankton encounter when falling through water. Note that $a = 1$, $b = 2$, and $c = 3$ are constants that describe the dimensions of the plankton.

Find a value of M for which $\int_1^M \frac{dx}{\sqrt{(a^2+x)(b^2+x)(c^2+x)}}$ differs from the original model of resistance by at most 0.001. *Hint:* make use of the integral $\int_M^{\infty} \frac{dx}{\sqrt{(a^2+x)(b^2+x)(c^2+x)}}$ and the comparison test.