

4. [12 points] The function $f(x) = \int_0^x 10e^{-t^2} dt$ appears frequently in statistical analysis.
- a. [6 points] Without calculating them, order $\int_0^2 f(x)dx$, MID(4), and TRAP(4) from smallest to biggest, where MID(4) and TRAP(4) are approximations for $\int_0^2 f(x)dx$. Show all work to justify your answer.

- b. [2 points] Consider the following table, which evaluates $f(x) = \int_0^x 10e^{-t^2} dt$ for the specified values of x .

| | | | | | |
|--------|---|-------|-------|-------|---|
| x | 0 | 0.5 | 1 | 1.5 | 2 |
| $f(x)$ | A | 4.613 | 7.468 | 8.562 | B |

What are the values of A and B? Write your answers on the spaces provided, rounding to three decimal places.

A = _____ B = _____

- c. [4 points] Using the table provided in part (b) and the answers you found in part (b), calculate LEFT(4) and RIGHT(4) to estimate the integral $\int_0^2 f(x)dx$. Be sure to show enough work to support your answer.