2. [17 points]

The graph of an odd function $f$ is shown below.

a. [7 points] Let $F(x)$ be the antiderivative of $f(x)$ with the property that $F(3)=-2$. Use the graph of $f(x)$ to compute the following values of $F(x)$.

| $x$ | -7 | -6 | -3 | 0 | 3 | 6 | 7 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $F(x)$ |  |  |  |  |  |  |  |

Solution: | $x$ | -7 | -6 | -3 | 0 | 3 | 6 | 7 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $F(x)$ | 1 | 0 | -2 | 0 | -2 | 0 |

b. [8 points] Sketch the graph of $F(x)$ from $x=-7$ to $x=7$. Label all points of inflection.

c. [2 points] Calculate the average value of $f$ between $x=-3$ and $x=7$.

Solution: $\frac{1}{7-(-3)} \int_{-3}^{7} f(x) d x=\frac{3}{10}$

