1. [16 points] At a time $t$ seconds after a catapult throws a rock, the rock has horizontal velocity $v(t) \mathrm{m} / \mathrm{s}$. Assume $v(t)$ is monotonic between the values given in the table and does not change concavity.

$$
\begin{array}{c|c|c|c|c|c|c|c|c|c}
t & 0 & 1 & 2 & 3 & 4 & 5 & 6 & 7 & 8 \\
\hline v(t) & 47 & 34 & 24 & 16 & 10 & 6 & 3 & 1 & 0
\end{array}
$$

a. [4 points] Estimate the average horizontal velocity of the rock between $t=2$ and $t=5$ using the trapezoid rule with 3 subdivisions. Write all the terms in your sum. Include units.
b. [4 points] Estimate the total horizontal distance the rock traveled using a left Riemann sum with 8 subdivisions. Write all the terms in your sum. Include units.
c. [4 points] Estimate the total horizontal distance the rock traveled using the midpoint rule with 4 subdivisions. Write all the terms in your sum. Include units.
d. [4 points] A second rock thrown by the catapult traveled horizontally 125 meters. Determine whether the first rock or the second rock traveled farther, or if there is not enough information to decide. Circle your answer. Justify your answer.
the first rock the second rock not enough information

