

6. [10 points] The Rodin Coil is a fantastic device that (supposedly) creates unlimited free energy. The rate at which it creates this energy is a function of the volume of the coil.
- a. [5 points] Suppose a prototype of the Rodin Coil is the solid whose base is the circle  $x^2 + y^2 = 2$  (where  $x$  and  $y$  are measured in meters), and whose cross sections perpendicular to the  $x$ -axis are squares. Write, but do **not** compute, an expression involving one or more integrals which gives the volume, in cubic meters, of this prototype.
- b. [5 points] One of Rodin's students was able to come up with an even more efficient free energy machine. Suppose the student's prototype was made by taking the same circle  $x^2 + y^2 = 2$  and rotating it around the vertical line  $x = 3$ . Write, but do **not** compute, an expression involving one or more integrals which gives the volume, in cubic meters, of this prototype.