

8. [14 points] Let $g(x)$ be a differentiable function with domain $(-1, 10)$ where some values of $g(x)$ and $g'(x)$ are given in the table below. Assume that all local extrema and critical points of $g(x)$ occur at points given in the table.

x	0	1	2	3	4	5	6	7	8
$g(x)$	2.0	3.3	5.7	6.8	6.0	4.3	2.4	0.2	-4.9
$g'(x)$	2.8	2.5	2.0	0.0	-1.4	-1.9	-1.6	-3.0	-8.1

- a. [3 points] Estimate $\int_0^8 g(x) dx$ using RIGHT(4). Write out each term in your sum.

- b. [4 points] Approximate the area of the region between $g(x)$ and the function $f(x) = x + 2$ for $0 \leq x \leq 4$, using MID(n) to estimate any integrals you use. Use the greatest number of subintervals possible, and write out each term in your sums.

- c. [3 points] Is your answer to **b.** an overestimate, an underestimate, or is there not enough information to tell? Briefly justify your answer.

Answer: (circle one)

OVERESTIMATE

UNDERESTIMATE

NOT ENOUGH INFORMATION

- d. [4 points] Write an integral giving the arc length of $y = g(x)$ between $x = 2$ and $x = 8$. Estimate this integral using TRAP(2). Write out each term in your sum.

Answer: Integral: _____

Answer: TRAP(2)= _____