8. [12 points] Consider the region $\mathcal{R}$ bounded by the curve $x^{2}+3 y=4$ and the $x$-axis.

a. [4 points] Write an expression involving one or more integrals that gives the perimeter, in cm , of $\mathcal{R}$. You do not need to evaluate the integral.


#### Abstract

Answer: b. [4 points] Write an expression involving one or more integrals that gives the volume, in $\mathrm{cm}^{3}$, of the solid formed by rotating $\mathcal{R}$ about the line $x=-4$.


#### Abstract

Answer: c. [4 points] Write, but do not evaluate, an expression involving one or more integrals that gives the mass, in grams, of a thin plate in the shape of the region R that has mass density given by $\delta(x)=x+2 \mathrm{~g} / \mathrm{cm}^{2}$.


Answer:

